

For discussion

How to Apportion Blame for a Queue with Arrivals in Bursts?

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Question

- What AQM marking best apportions blame for a queue with arrivals in bursts?

Answer so far (spoiler alert)

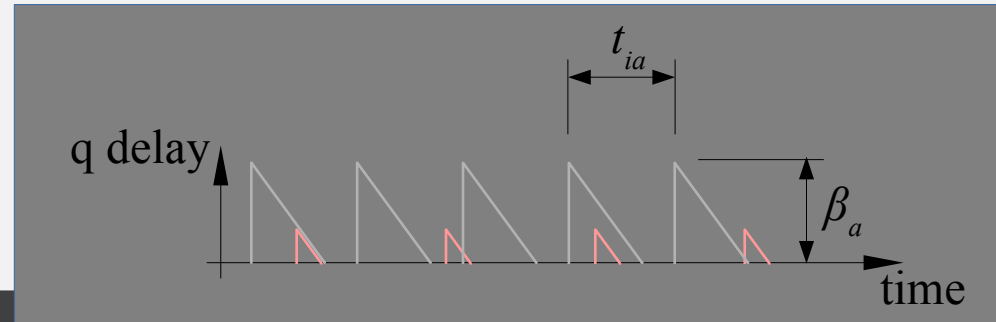
- Only marking packets, with no flow state
 - Arrivals in bursts can lead to a queue
 - even if they can be served on average
 - Subsequent smoother arrivals sit behind the burst
 - with knock-on impact on the next arrivals
 - even after the initial burst has all departed
- Definitely not sojourn marking
 - The alternative I thought would work is better but not good enough

Roadmap

- Question
- Explanation of approach
- Explanation of parameter space
- Results
- Evaluation
- Interpretation
- Implications & Next steps

Approach

- Propose marking approaches (see later), then compare
- Model? Simulate? Testbed?
 - model first: initial goal is understanding
 - noise of reality (packet sizing, timing dither, sync effects) could otherwise obstruct
- Unresponsive? Responsive?
 - unresponsive: cannot assume a response, so marking might solely drive policing*
- Simplest sufficient scenario; 2 flows, a & b , with:
 - constant but different burst sizes, β
 - constant but different capacity shares, λ
 - No need for either to vary (understand bursts first, not bursts of bursts)
- Reduces to 2 (sawtooth) waves with different amplitude β & wavelength (interval t_i)
 - capacity share, $\lambda = \beta / t_i$
 - any 1 of these 3 variables depends on the other 2



* might use flow state

Approach

Normalized metrics

Goal: results applicable to any link rate and any step marking threshold delay

- Burst size β is in units of time (queue delay)
 - normalized to: marking threshold = 1 unit of time
- On time series plots, time is also normalized
 - queue delay at marking threshold = 1 unit of time
- Marking probability, p , and capacity share, λ
 - both dimensionless and bounded within $[0,1]$
 - so normalized marking rate, λp , also bounded within $[0,1]$

Approach

Parameter space

- A full scan of all 4 dimensions:

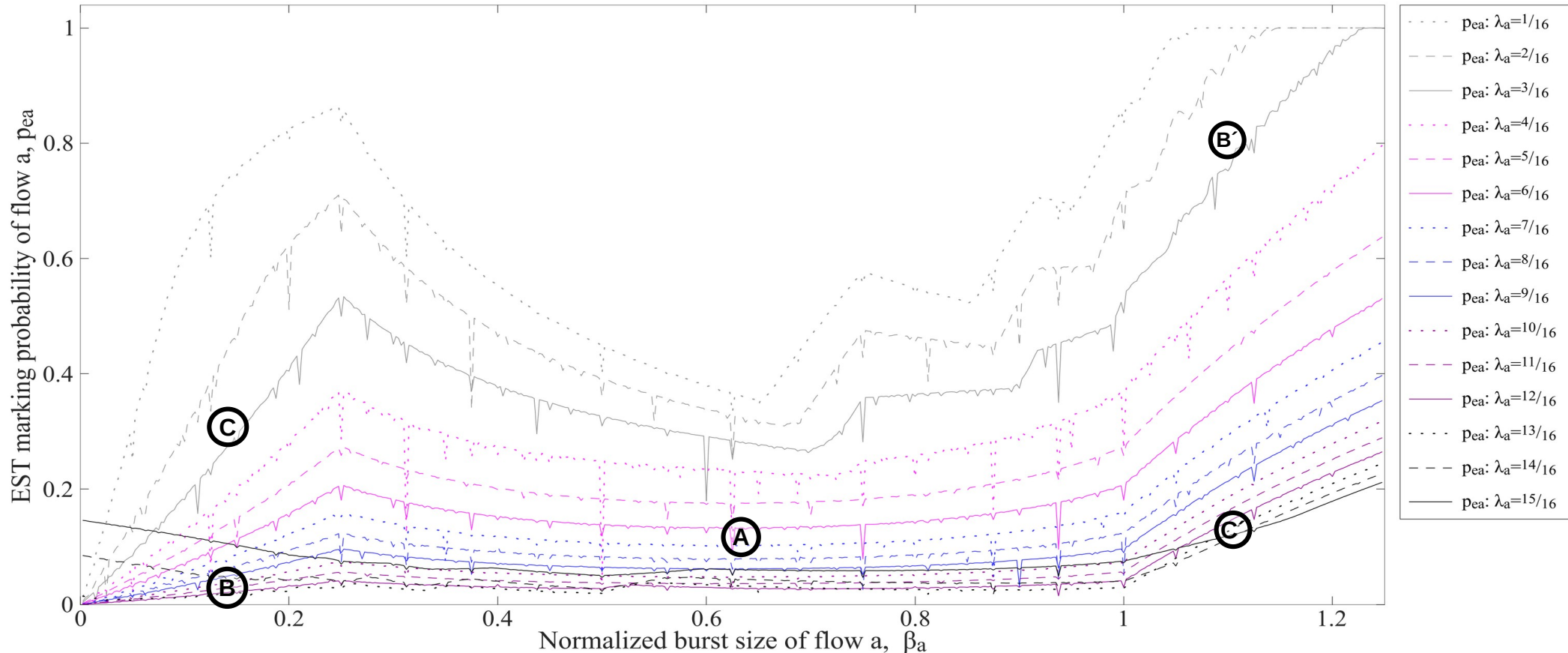
$$\beta_a, \lambda_a, \beta_b, \lambda_b$$

would generate more heat than light

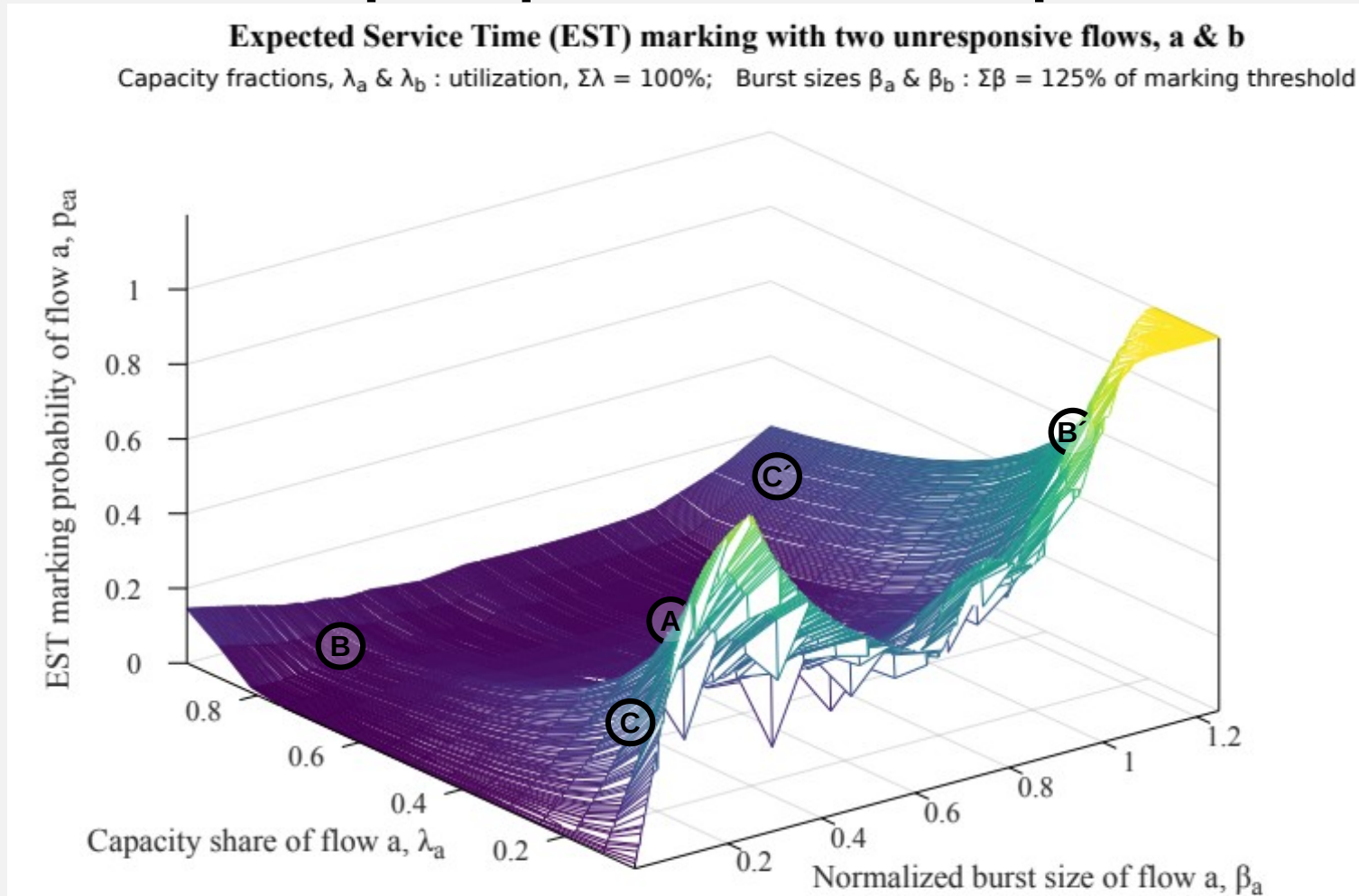
- To focus on apportioning blame, scan the parameter space of one flow (β_a, λ_a) , while trying to keep the whole system constant, i.e.
 - constrain $\Sigma\lambda$ (utilization) to a small selection of constants (assume $\Sigma\lambda \leq 1$)
 - constrain $\Sigma\beta$ (max total burst) to a small selection of constants
- Compare two marking approaches, based on the q delay...
 - ...a packet itself experiences (the queue ahead at enqueue)
 - ...a packet causes to others (the queue behind at dequeue)

How to Interpret the Parameter Space

Expected Service Time (EST) marking with two unresponsive flows, a & b
Capacity fractions, λ_a & λ_b : utilization, $\Sigma\lambda = 100\%$; Burst sizes β_a & β_b : $\Sigma\beta = 125\%$ of marking threshold



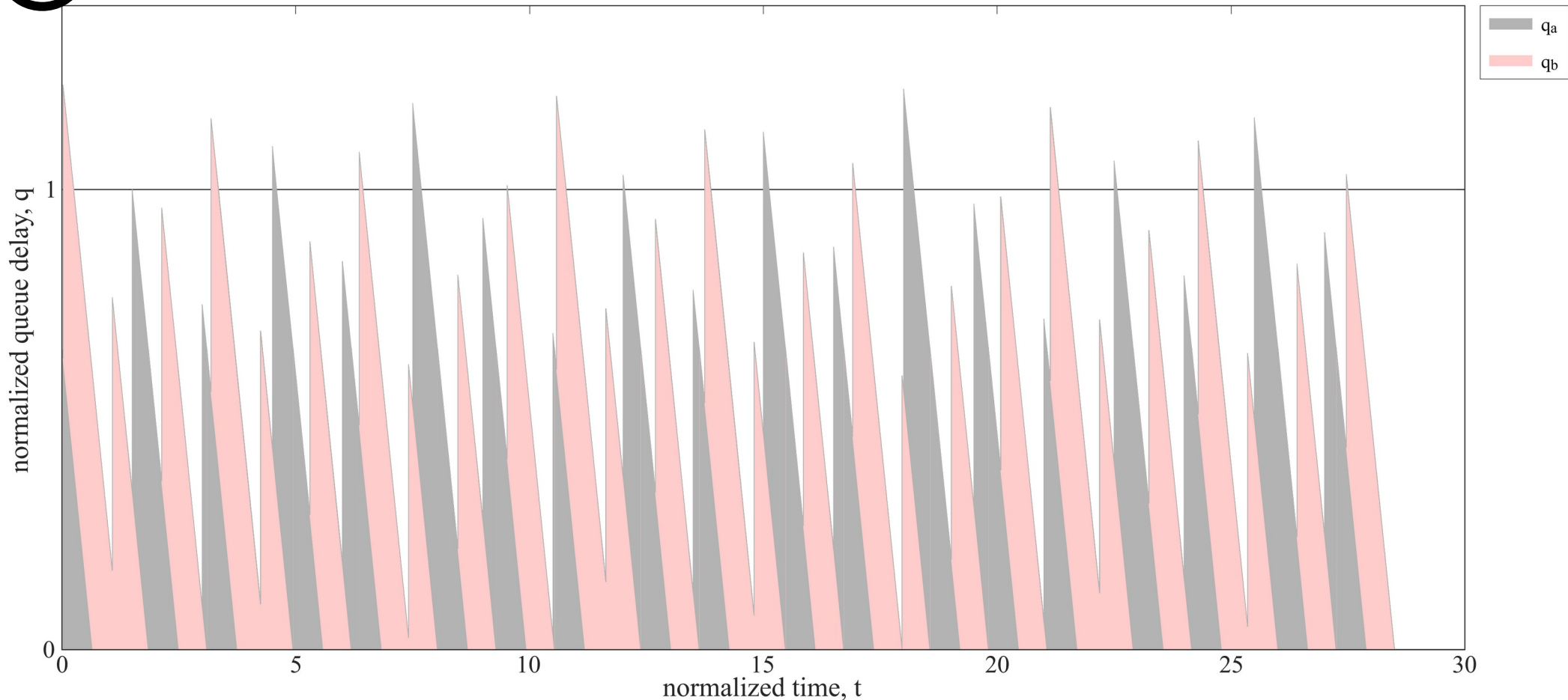
Same example parameter space in 3-D



A

Two unresponsive flows, a & b; Phase shift, $\phi = 3.0864\%$

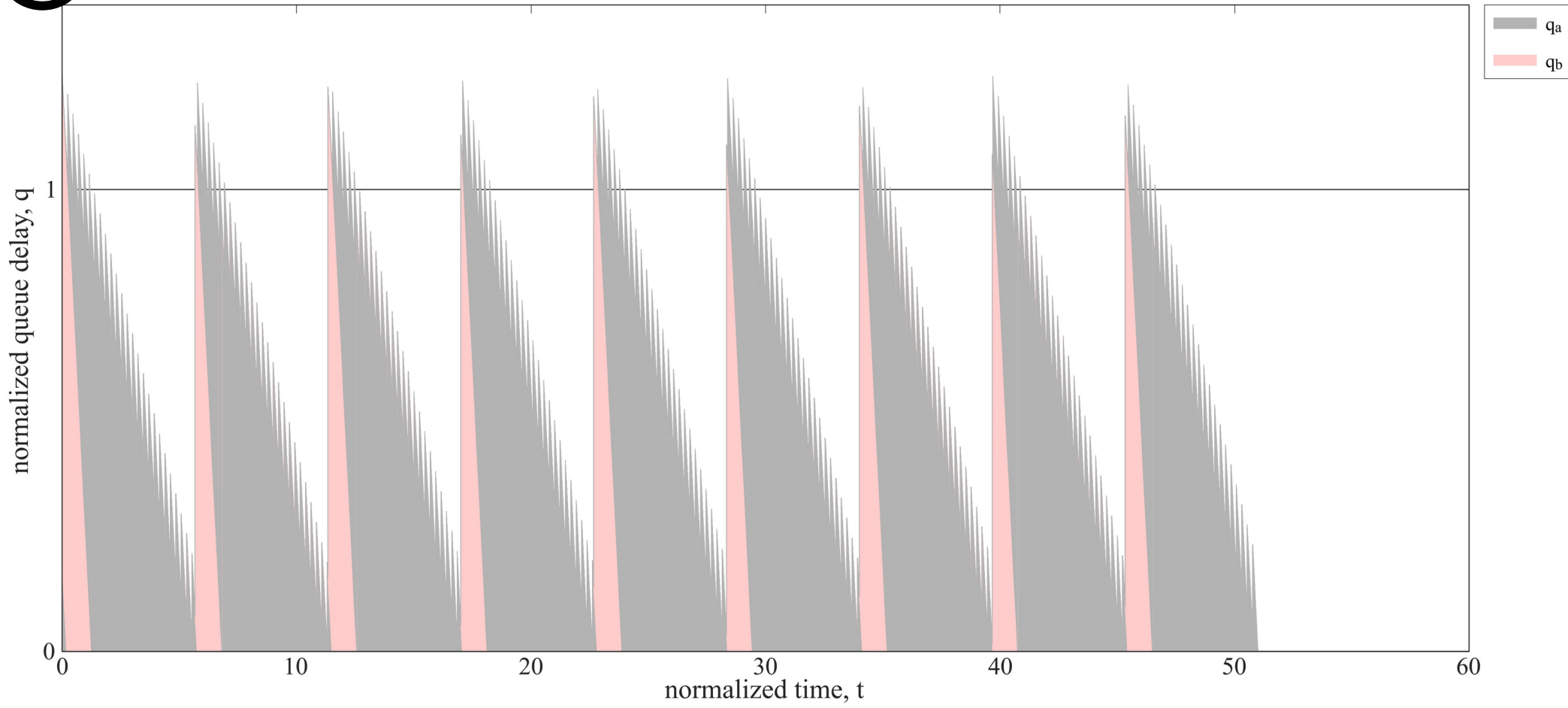
Capacity fractions, $\lambda_a = 7/16, \lambda_b = 9/16$ ($\Sigma\lambda = 100\%$); Burst queue delays $\beta_a = 65.625\%, \beta_b = 59.375\%$ ($\Sigma\beta = 125\%$)

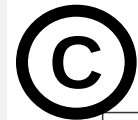


B

Two unresponsive flows, a & b; Phase shift, $\phi = 3.0864\%$

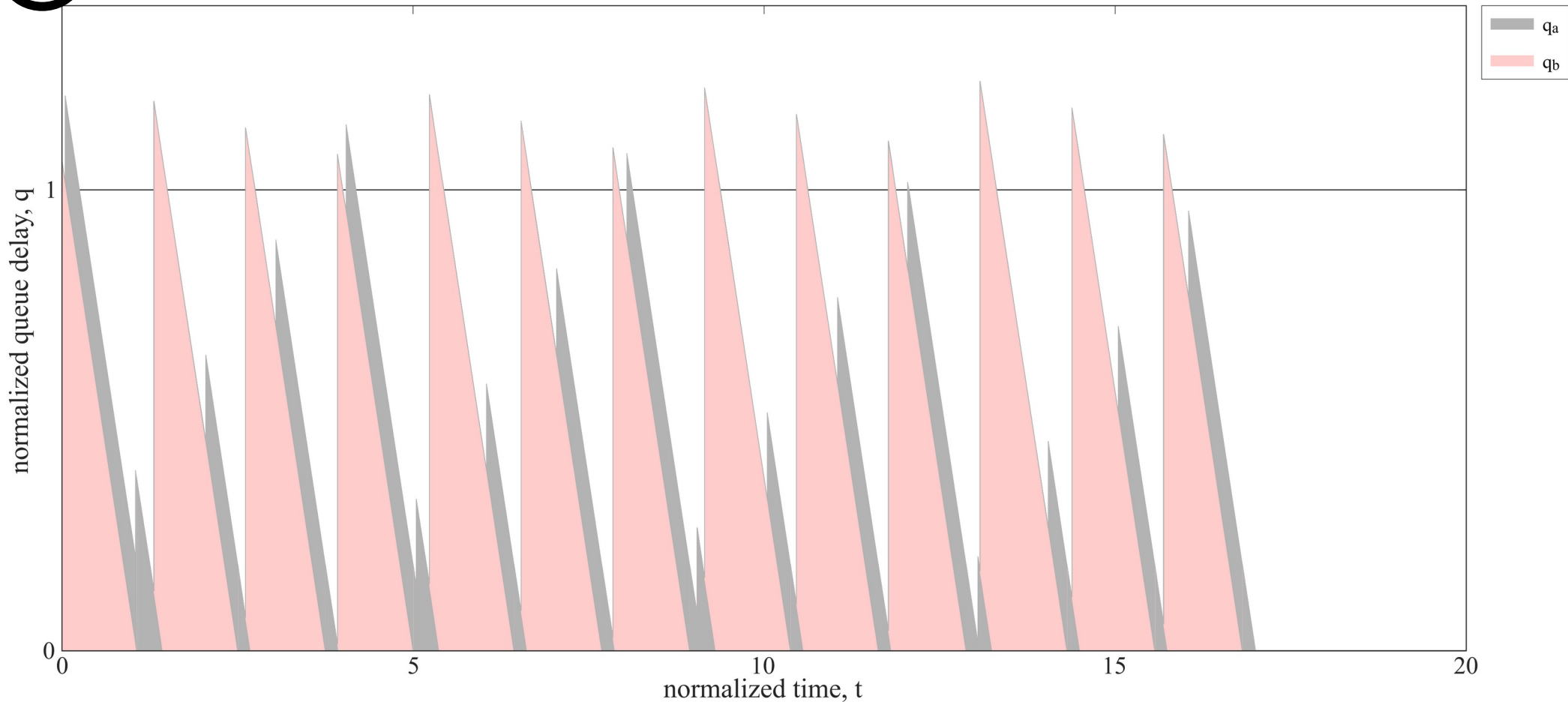
Capacity fractions, $\lambda_a = 13/16$, $\lambda_b = 3/16$ ($\Sigma\lambda = 100\%$); Burst queue delays $\beta_a = 18.75\%$, $\beta_b = 106.25\%$ ($\Sigma\beta = 125\%$)





Two unresponsive flows, a & b; Phase shift, $\phi = 3.0864\%$

Capacity fractions, $\lambda_a = 3/16$, $\lambda_b = 13/16$ ($\Sigma\lambda = 100\%$); Burst queue delays $\beta_a = 18.75\%$, $\beta_b = 106.25\%$ ($\Sigma\beta = 125\%$)



Ideals for apportioning blame

- Marking probability of one flow, p_a
 - 1) should monotonically increase with its burst size, β_a
 - 2) should not decrease with its capacity share, λ_aassuming the whole system is otherwise constant
- Satisfying both ideals would be robust but probably unattainable, e.g.
 - would fail on #1 if marking saturates, e.g. v large bursts
 - unsure if #2 is even satisfied with equal constant burstiness (see control expt later)
- Some scope to relax either ideal,
 - but unable to quantify precisely, so far

Compare 2 marking approaches

- based on delay to self, q_s
 - sojourn-based marking (subscript s)
 - queue delay ahead at enqueue
 - visualization: the amount and flow colour of the q over the threshold
- based on delay to others, q_e
 - expected service time (subscript e)
 - queue delay behind at dequeue
 - visualization: colour of flow being dequeued when the q is over threshold

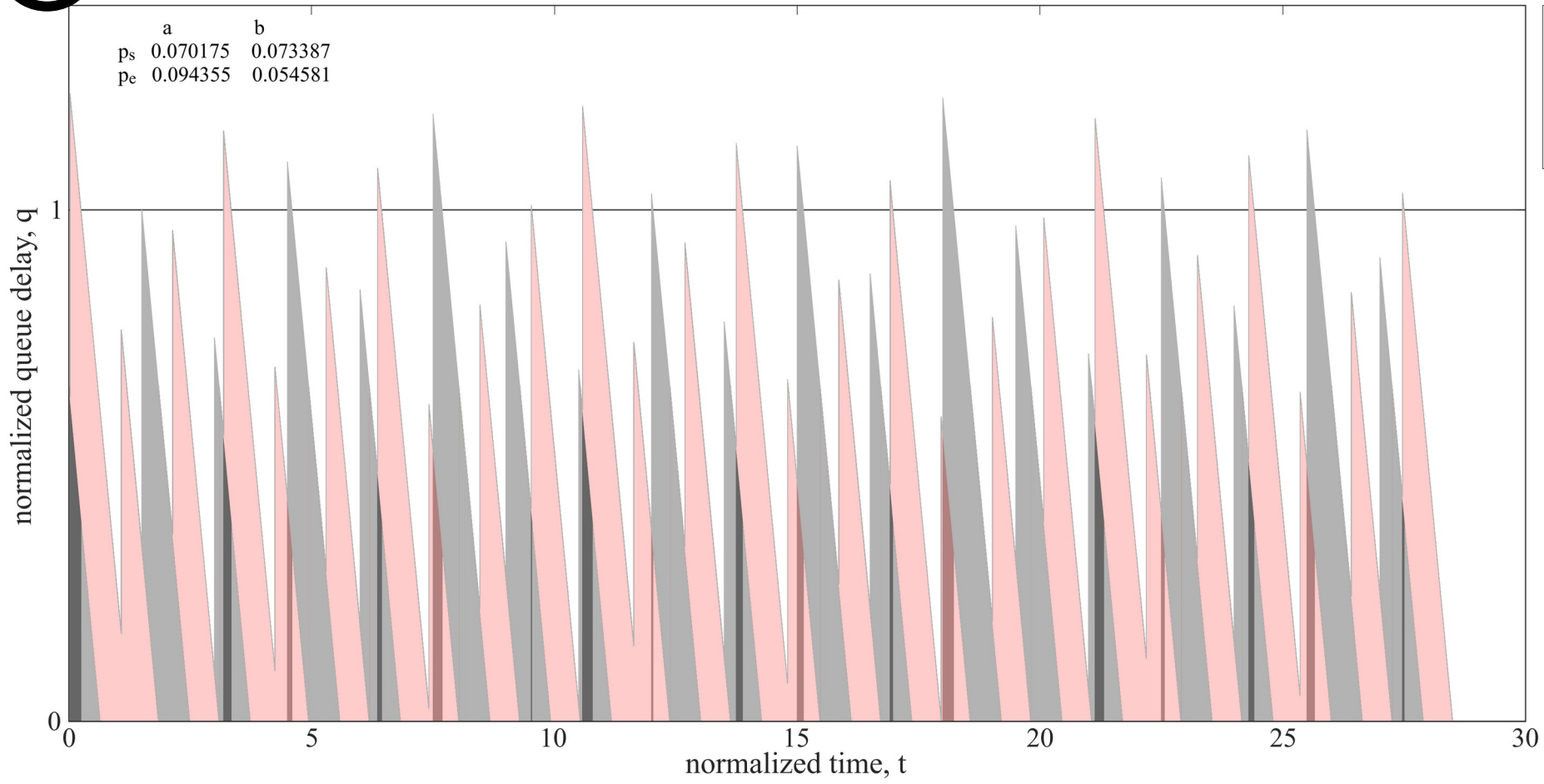
A

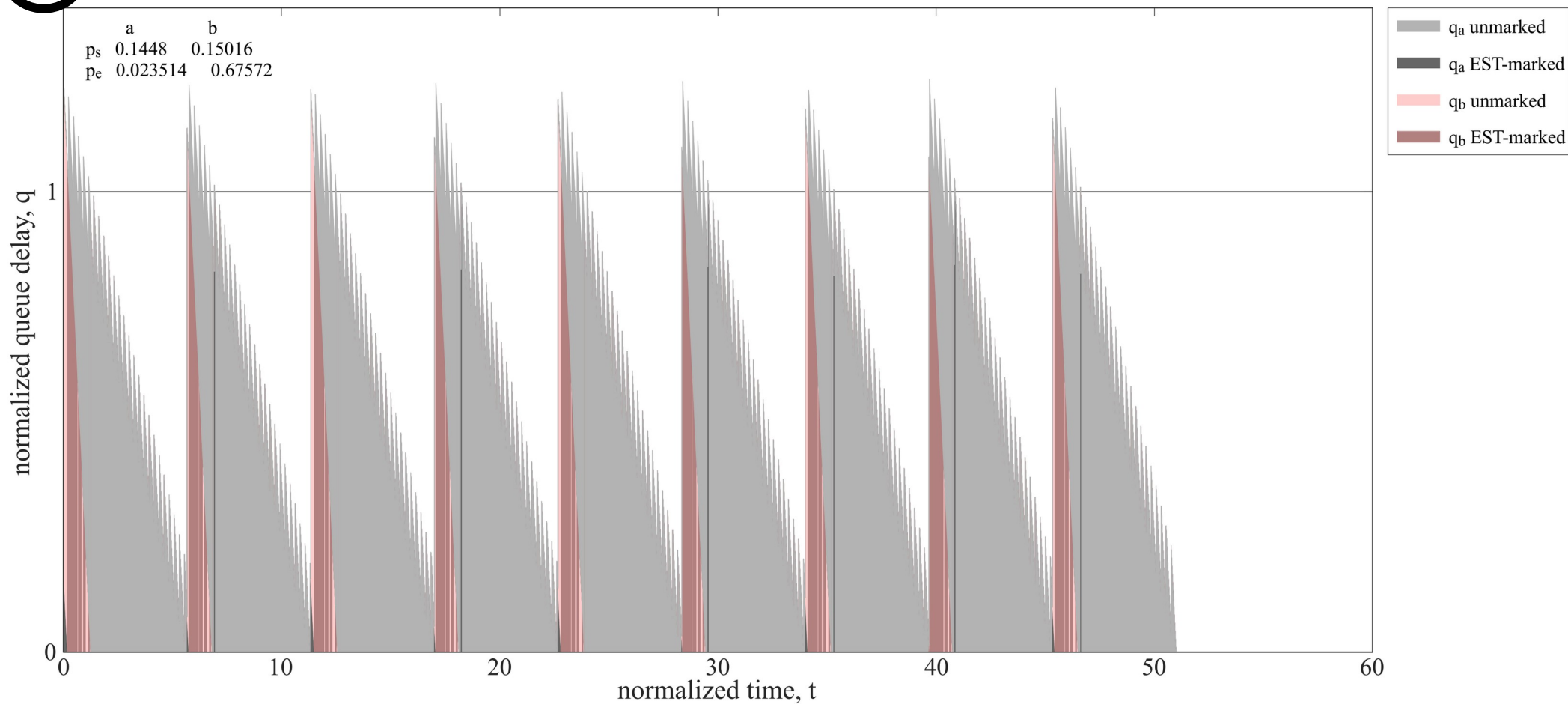
Two unresponsive flows, a & b; Phase shift, $\phi = 3.0864\%$

Capacity fractions, $\lambda_a = 7/16, \lambda_b = 9/16$ ($\Sigma\lambda = 100\%$); Burst queue delays $\beta_a = 65.625\%, \beta_b = 59.375\%$ ($\Sigma\beta = 125\%$)

	a	b
p_s	0.070175	0.073387
p_e	0.094355	0.054581

- q_a unmarked
- q_a EST-marked
- q_b unmarked
- q_b EST-marked



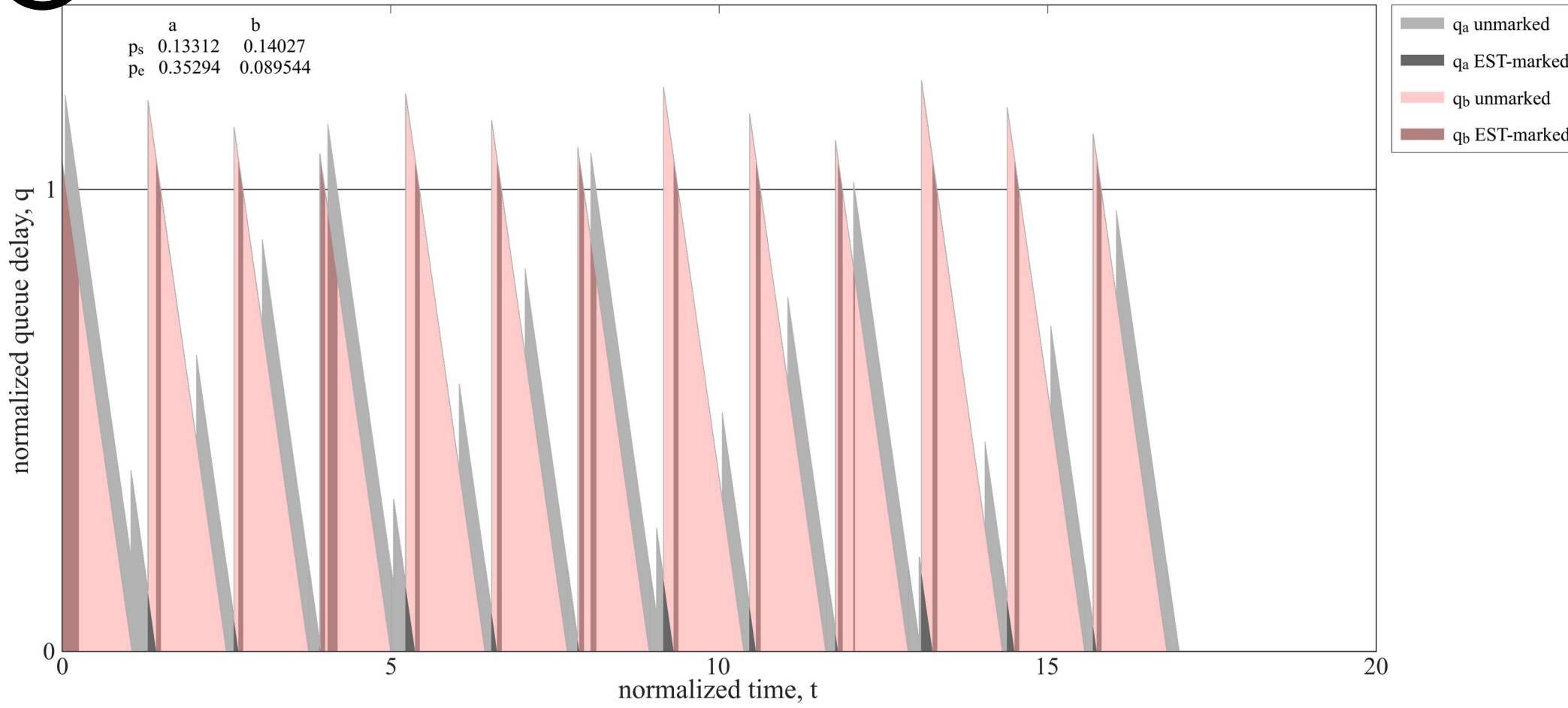
B**Two unresponsive flows, a & b;**Phase shift, $\phi = 3.0864\%$ Capacity fractions, $\lambda_a = 13/16$, $\lambda_b = 3/16$ ($\Sigma\lambda = 100\%$);Burst queue delays $\beta_a = 18.75\%$, $\beta_b = 106.25\%$ ($\Sigma\beta = 125\%$)



Two unresponsive flows, a & b; Phase shift, $\phi = 3.0864\%$

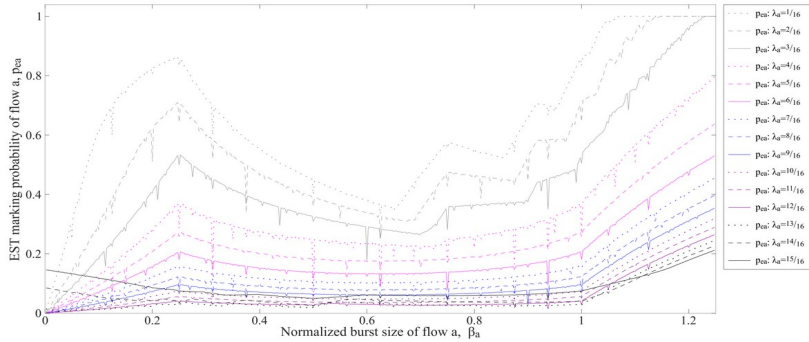
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	a	b
p_s	0.13312	0.14027
p_e	0.35294	0.089544



Results – Examples

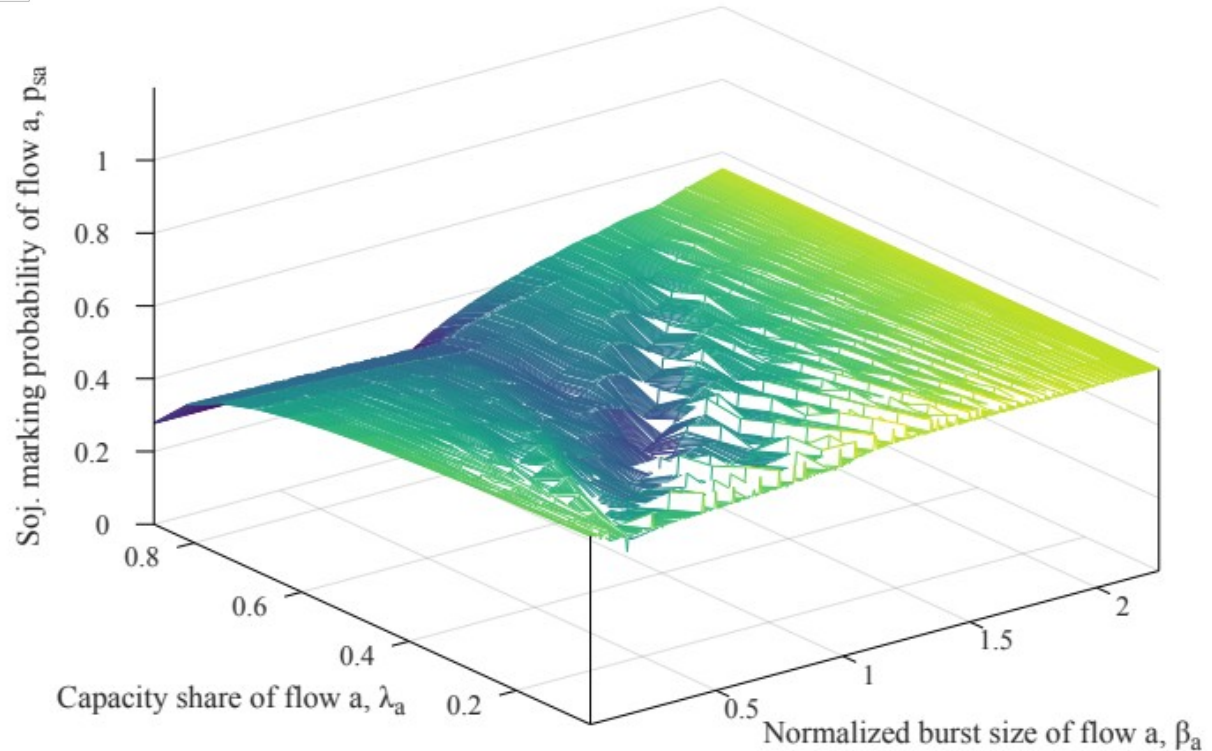
Expected Service Time (EST) marking with two unresponsive flows, a & b
Capacity fractions, λ_a & λ_b : utilization, $\Sigma\lambda = 100\%$; Burst sizes β_a & β_b : $\Sigma\beta = 125\%$ of marking threshold



- Detailed 2-D plots (like above)
 - in 4 complementary slide packs
 - 1 for each metric
- choice of 4 metrics
 - p_a : marking probability of flow a
 - $\Delta p = p_a - p_b$
 - $\lambda_a p_a$: marking rate of flow a
 - $\Delta(\lambda p) = \lambda_a p_a - \lambda_b p_b$
- Next 2 slides: 3-D plots
 - using first metric only (p_a)
 - axes will be too small to read, but all like the example to the right

Sojourn marking with two unresponsive flows, a & b

Capacity fractions, λ_a & λ_b : utilization, $\Sigma\lambda = 93.75\%$; Burst sizes β_a & β_b : $\Sigma\beta = 225\%$ of marking threshold



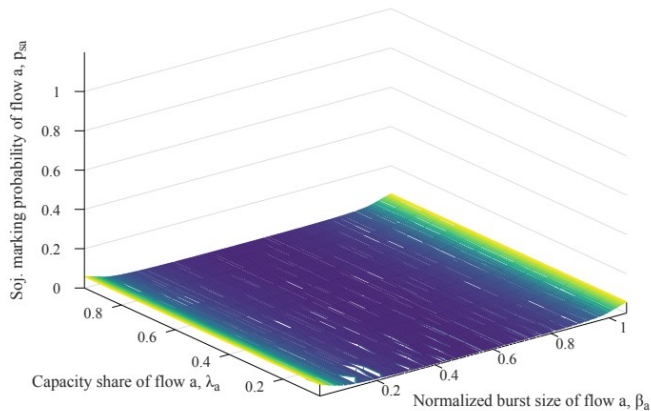
Sojourn marking

utilization, $\Sigma\lambda$

100%

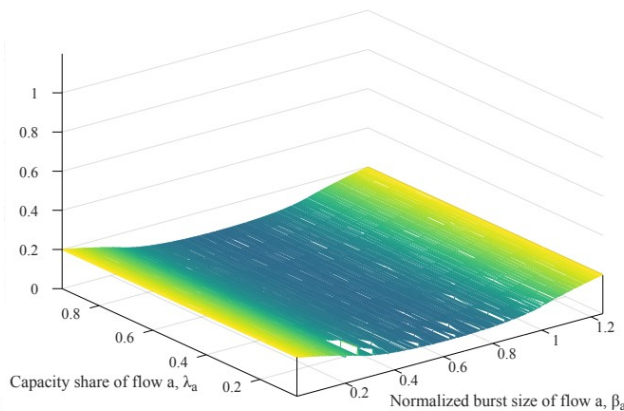
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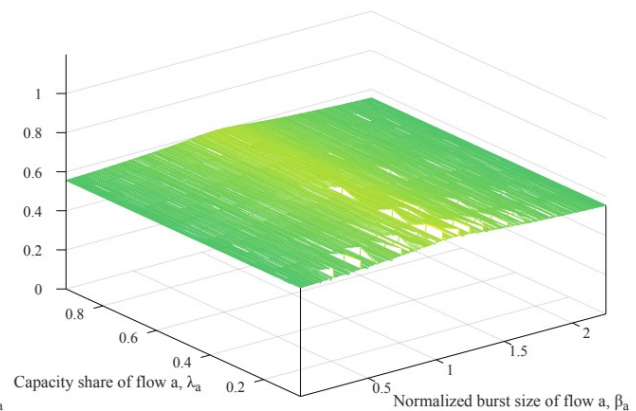
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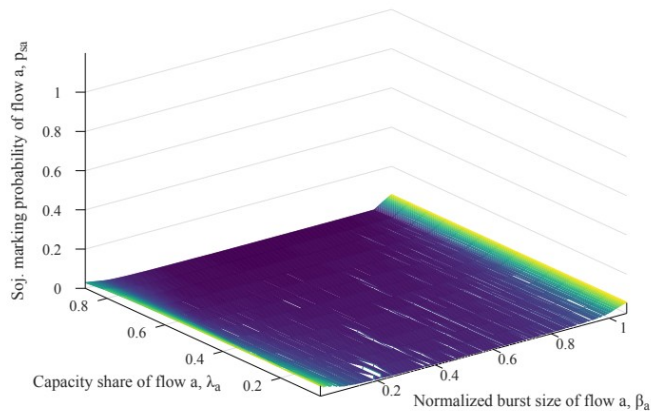
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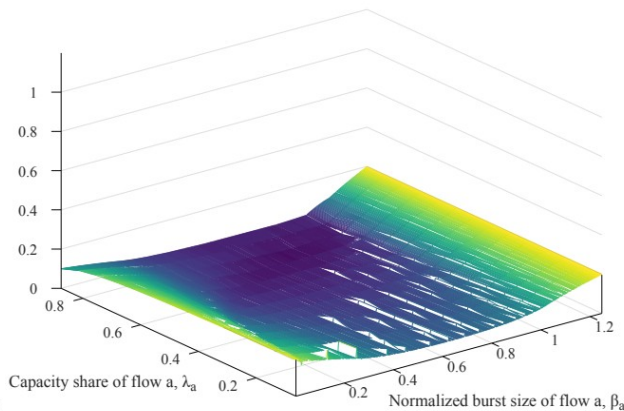
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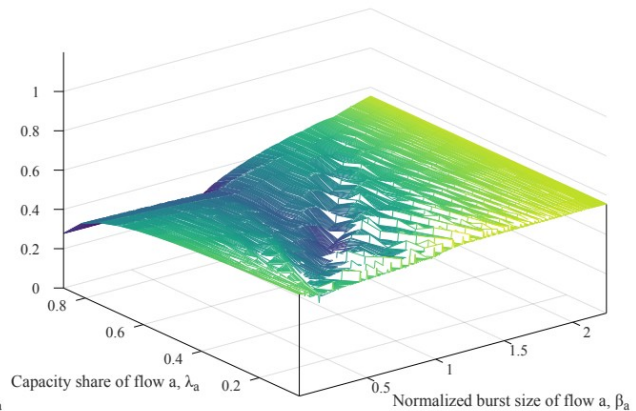
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93.75%

max burst, $\Sigma\beta$

106.25%

125%

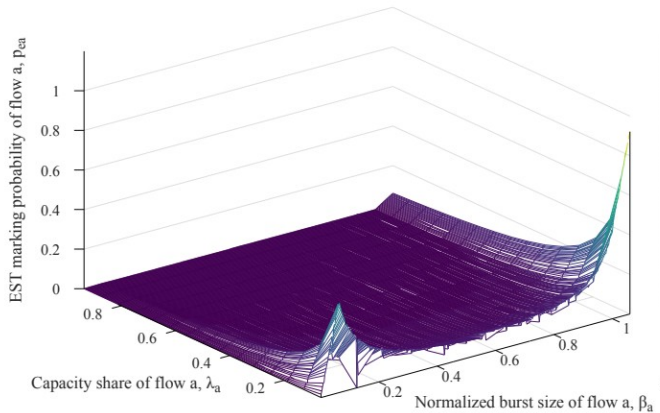
225%

EST marking

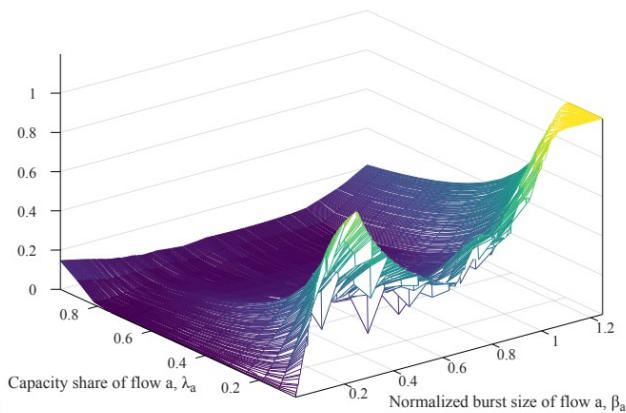
utilization, $\Sigma\lambda$

100%

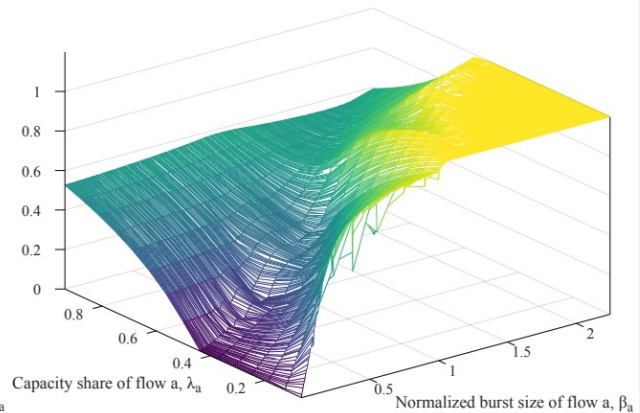
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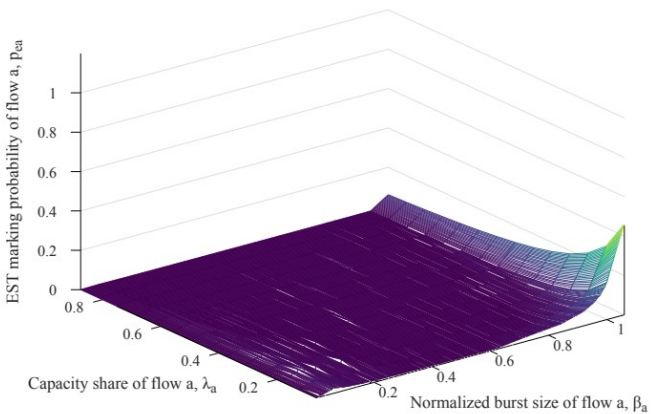
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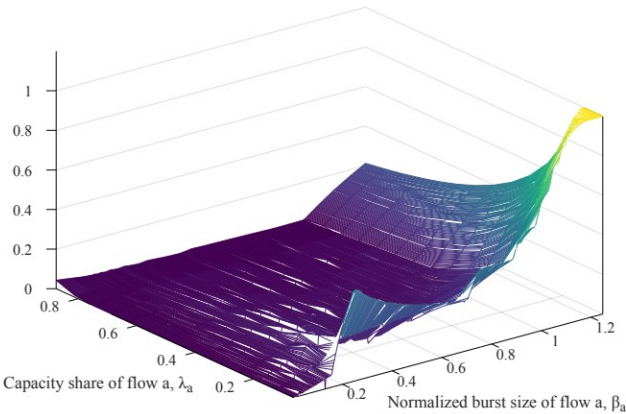
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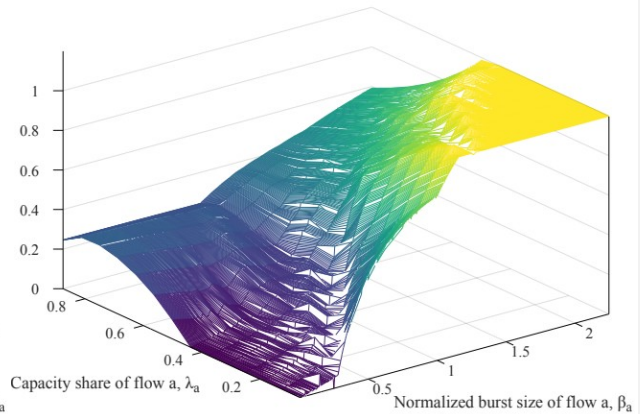
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93.75%

max burst, $\Sigma\beta$

106.25%

125%

225%

"Traffic-Light" Evaluation

ideal:	increase with burst size β_a ?	not decrease with capacity share λ_a ?
sojourn ¹	N ²	Y ¹
EST	Y & N ³	N

- Sojourn is not good enough, but EST is not sufficiently better to replace it
- Not as clear-cut as the "traffic light" colours imply
 - see earlier: "some scope to relax either ideal"
 - but "unable to quantify precisely, so far"

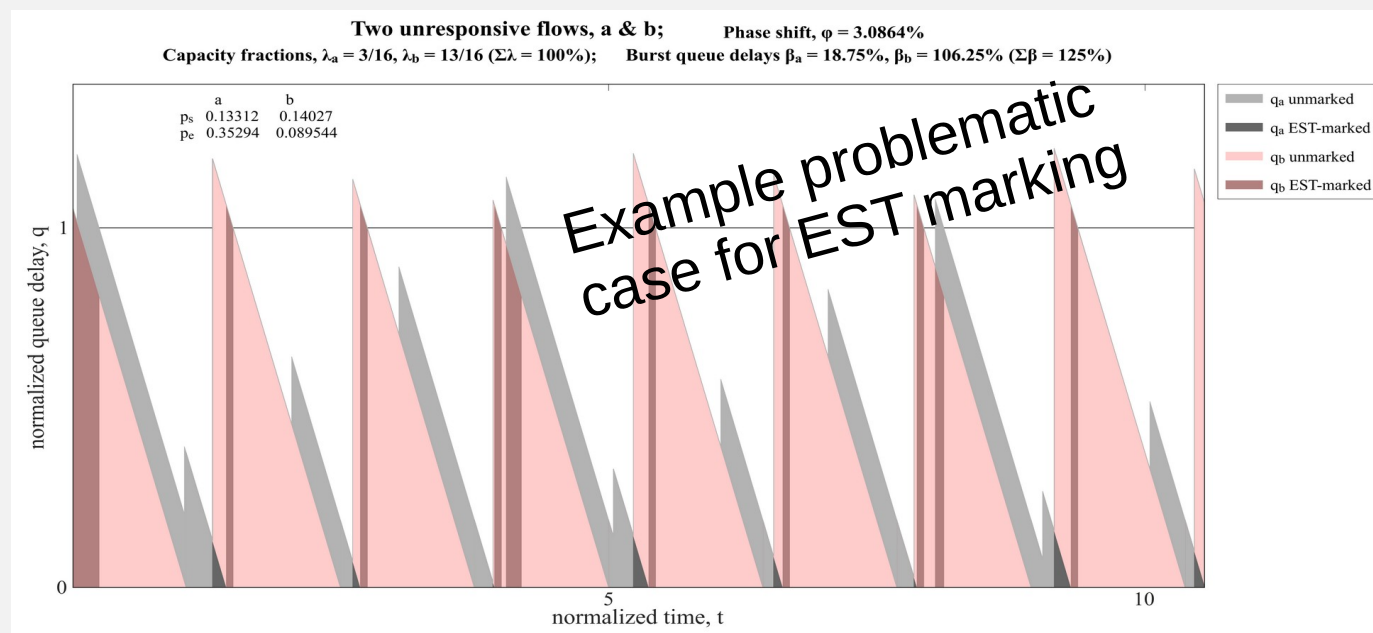
¹ in general, other than high max burst and low utilization

² symmetric about the avg burst size

³ decreases from a peak at $\beta_a = \Sigma\beta - 1$ if low capacity share

Why EST is not a panacea

- for a grey flow with low capacity share and smaller bursts than pink
- even though grey arrives smoothly, it can only depart in the gaps betw. pink bursts
- variation in these gaps and in how many grey bursts arrive between pink ones is high relative to average grey traffic
- EST marks the residual grey in the q when the next pink burst arrives
- and the pink burst gets pushed back, closing subsequent gaps
- **on average grey fits between pink bursts, but EST punishes grey for all variance**



Next steps

- Design a better marking approach?
 - using the insights from this research
 - based on sthg like $q_e - q_s$. Perhaps $2(q_e - q_s)(q_e + q_s)$?
- Validate model against:
 - ns3 simulation
 - testbed
- Design and evaluate an aggregate policer?

More information

- These slides, full results, simulator code
 - <https://github.com/bbriscoe/l4s-aqm/blob/master/papers/working/README.md>
 - Note: pls ignore current version of tech report
 - written before this latest work

How to Apportion Blame for a Queue with Arrivals in Bursts?

Discussion
and spare slides

Experiment plans

Revisit
Original

✓ Expt 1.1:

- For a set of fixed capacity shares $\lambda_a + \lambda_b = \Sigma\lambda$ (constant)
- burst size β : increase β_a , decrease β_b , with $\beta_a + \beta_b = \Sigma\beta$ (constant)
- measure both marking probabilities, p_s & p_e
- for each approach, report mean, max & min of each marking metric over a range of phase shifts

✓ Control expt 1.2:

- Same as #1.1, with $\Sigma\lambda$ and $\Sigma\beta$ constant
- but with $\beta_a = \beta_b$ increase λ_a
- marking should not depend on capacity share, λ
- **(can visualize this on 3-D plots of expt 1.1)**

• Expt 2.1:

- Same as #1.1, except hold β_b , while increasing β_a

✓ Expt 3.1:

- Same as #1.1 except increase β_a with λ_a
- **(can visualize this on 3-D plots of expt 1.1)**

- Expt 4? Model packetization or use ns3
- Redesign marking?
- Design & Model aggregate policer

Approach – more detail

Phase Shift

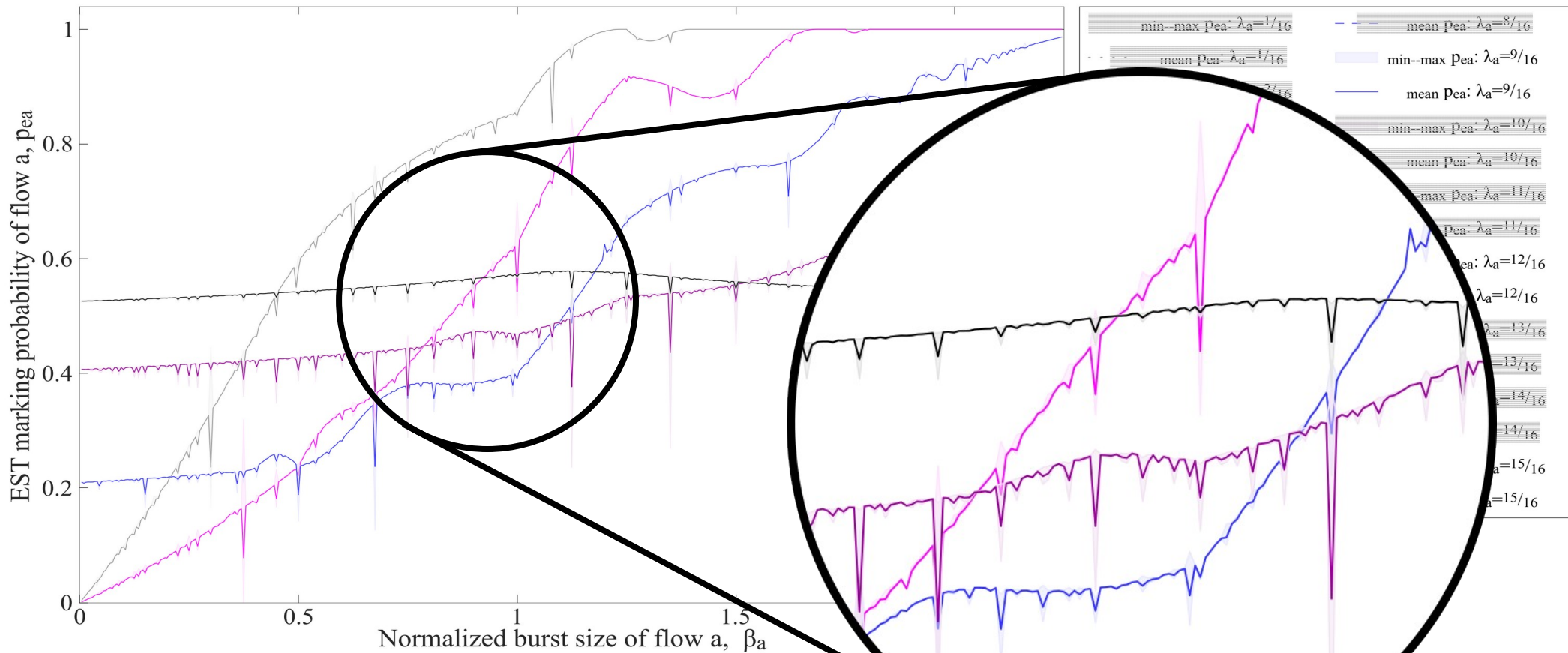
- At each point in the parameter space, start from multiple different phase shifts
- Avoid always including zero as one phase shift
- Record mean, max & min* of marking metrics

* variation is not symmetric, so std. dev. not applicable

Typical Spread of Results over 8 phase samples

Expected Service Time (EST) marking with two unresponsive flows, a & b

Capacity fractions, λ_a & λ_b : utilization, $\Sigma\lambda = 100\%$; Burst sizes β_a & β_b : $\Sigma\beta = 225\%$ of marking threshold



Interpretation: phase shift results

- points where spread increases are where the pattern repeats after a few bursts
 - i.e. lowest common integer multiple of the two burst intervals is low
 - then "law of large numbers" doesn't apply
 - unusual coincidences more likely, e.g. bursts never precisely coincide
- flows are unlikely to get stuck at these points
 - lower marking causes flow to increase window
- recommend a little randomization of burst sizing – just in case

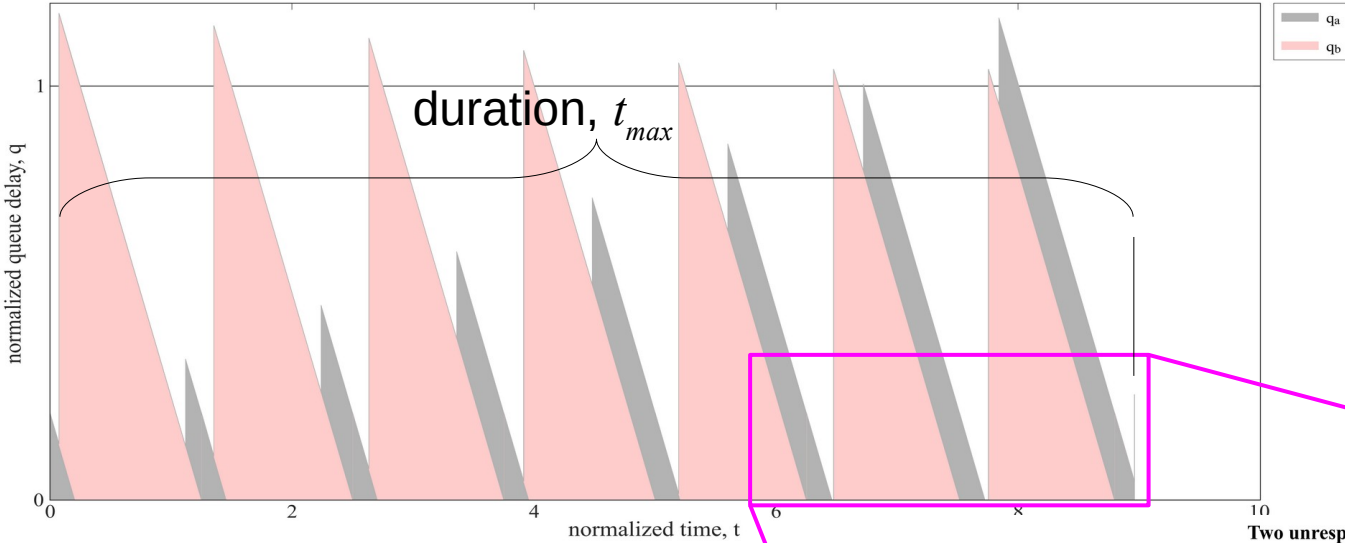
Approach – more detail

Minimal Repeating Pattern

- Duration: lowest common integer multiple
 - of the two burst intervals (not integers themselves)
- Find where to start
 - assume a sufficient standing queue to never go idle
 - start 2nd pass where standing q is smallest
 - challenge: 2 passes without doubling the run time

* variation is not symmetric, so std. dev. not applicable

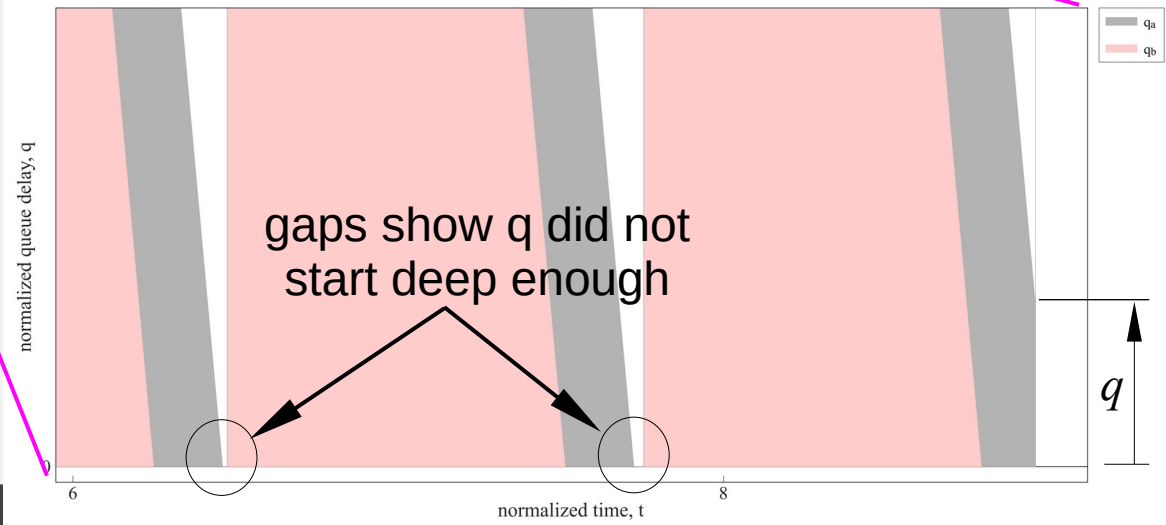
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Example of $q=0$ at the wrong burst

- if set $q = 0$ at wrong burst, $q > 0$ at end of duration and starting with a slightly larger q has a knock-on effect next round
- for correct approach see source (after 2 subtly incorrect attempts)

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Approach

What if's

- Check the validity of the approach, by investigating alternative avenues
 - increase burstiness of flow a, β_a , while holding β_b at a small selection of const. values
 - increase λ_a & β_a together, related by a selection of factors, e.g. $\Delta\lambda = k\Delta\beta$ (different diagonal paths across the 3-D surface)
 - investigate including zero in the range of phase shifts